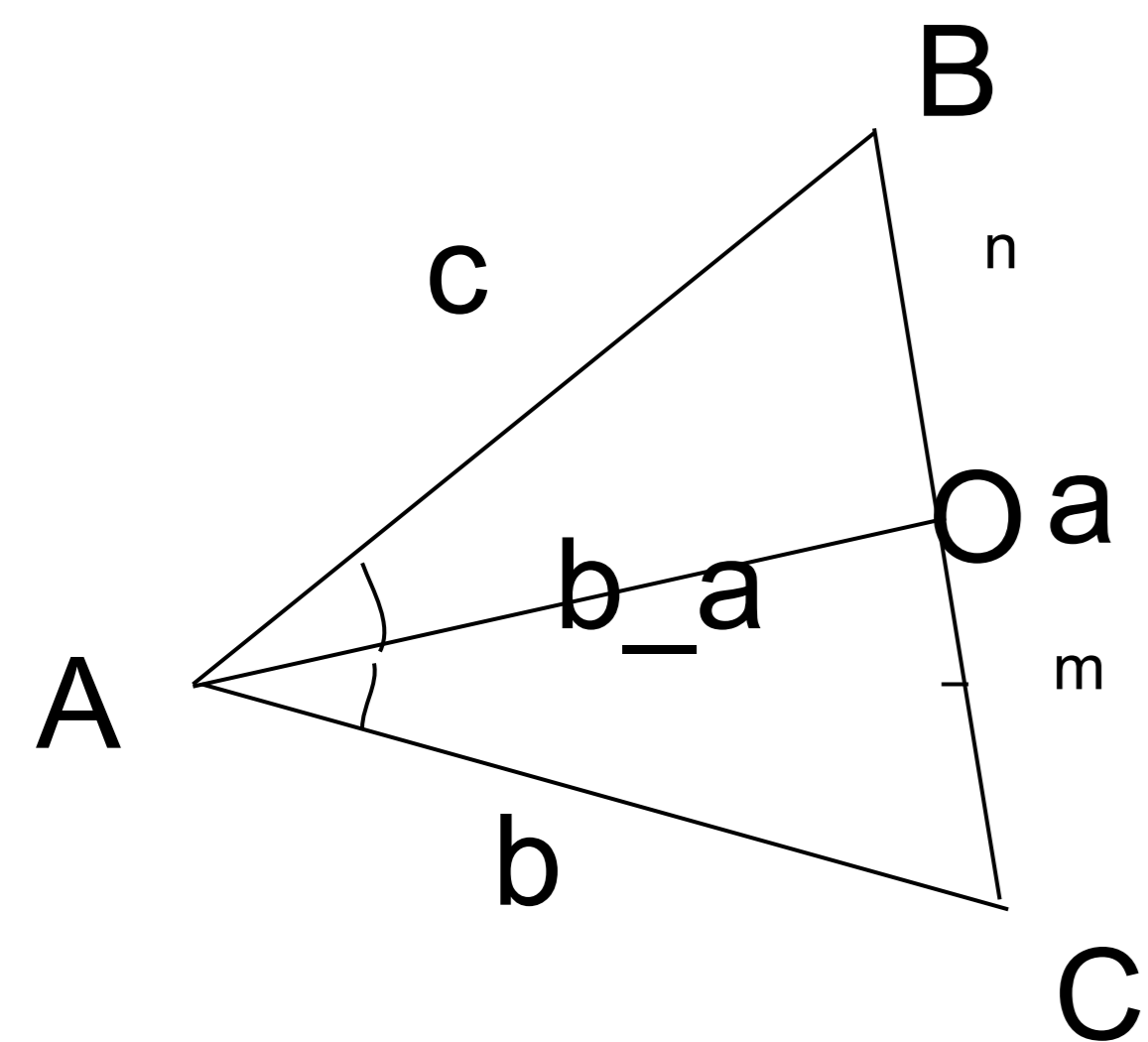


Дан треугольник ABC, и три его стороны a,b,c. найти  $b_a$



$S = \frac{1}{2} * ab * \sin(e)$  Док-во:

$$S = \frac{1}{2} * b * h$$

$$\sin e = h/a$$

$$h = \sin e * a$$

$$S = \frac{1}{2} * b * \sin e * a$$

$$S = \frac{1}{2} * ab * \sin(e)$$

Решение задачи

$$S(AOB) = \frac{1}{2} * c * b_a * \sin(BAO)$$

$$S(AOC) = \frac{1}{2} * b * b_a * \sin(CAO)$$

$$S1(ABC) = (b * \sin(CAO) + c * \sin(BAO)) * \frac{1}{2} * b_a$$

$$S2(ABC) = \frac{1}{2} * c * b * \sin(A)$$

$$\frac{1}{2} * c * b * \sin(A) = (b * \sin(A/2) + c * \sin(A/2)) * \frac{1}{2} * b_a$$

$$c * b * \sin(A) = (b * \sin(A/2) + c * \sin(A/2)) * b_a$$

$$c * b * \sin(A) = (b + c) * b_a * \sin(A/2)$$

$$c * b * 2 * \sin(A/2) * \cos(A/2) = (b + c) * b_a * \sin(A/2)$$

$$2 * c * b * \cos(A/2) = (b + c) * b_a$$

$$(2 * c * b * \cos(A/2)) / (b + c) = b_a$$

$$\cos B = (a^2 + c^2 - b^2) / 2ac$$

$$\cos A = (b^2 + c^2 - a^2) / 2bc$$

$$\cos 2x = 2 \cos^2 x - 1$$

$$\cos A = 2 \cos^2(A/2) - 1$$

$$\cos^2(A/2) = (\cos A + 1) / 2$$

$$\cos(A/2) = \sqrt{[(\cos A + 1) / 2]} = \sqrt{[(b^2 + c^2 - a^2) / 2bc + 1] / 2}$$

$$\cos(A/2) = \sqrt{[(b^2 + c^2 - a^2 + 2bc) / 4bc]} = \sqrt{[(b + c)^2 - a^2] / 4bc} = \sqrt{[(b + c - a + a - a)(b + c + a) / 4bc]} = \sqrt{[(b + c + a) / 2 - a] * (b + c + a) / 2} / bc$$

$$(a + b + c) / 2 = p$$

$$\cos(A/2) = \sqrt{[(p - a) * p] / bc}$$

$$b_a = (2 * c * b * \cos(A/2)) / (b + c)$$

$$b_a = (2 * b * c * \sqrt{[(p - a) * p] / bc}) / (b + c)$$

$$b_a = (2 * \sqrt{[(p - a) * p * bc]}) / (b + c)$$

$$S = \frac{1}{2} * ab * \sin(e)$$

